



# A Quick Guide : English Version Multiplication Patterns

The Power of Ten system is based on the belief that the natural mode of the brain is to search for patterns. Noticing a pattern delivers a feeling of satisfaction – a feeling that something has been accomplished.

## Preparation for an **All the Facts** sheet

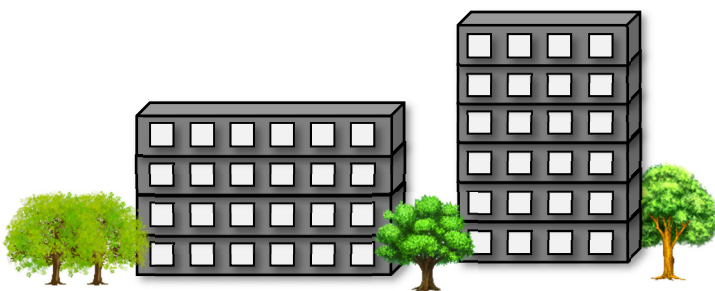
There are **132** math multiplication facts when the times tables for 0, 1, 2, 3 ...10 are listed.

The first major pattern that most children learn is that  $4 + 2$  gives the same answer as  $2 + 4$ . This is known as the **Principle of Conservation** and also known as the **Commutative Principle**. It is not important for students to know the names of this very important pattern, but it is one that is solidly embedded in the brain of students learning all their **adding** facts. Understanding and applying this pattern to the list of **132** facts cuts the list in half. If a student is memorizing the **multiplication** facts, then  $4 \times 6$  is different from  $6 \times 4$  and the arrays for these two **multiplication** facts are different in their orientation, but the same in their total amount (product).

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An apartment building with **4** floors and **6** apartments on each floor is different than an apartment building with **6** floors and **4** apartments on each floor – but they both have **24** apartments. This seems obvious, but it is a crucial and important pattern.

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Now that the list has been reduced from **132** facts to **66** facts, it is possible to know **45** of the **66** facts by patterns that are readily learned without any instruction. These **45** facts have been listed on the '**Multiplication Pattern Facts**' sheets. [\[See pages 3-6 of this document.\]](#)

The '**Multiplication Pattern Facts**' sheets have been created for students who find the **All the Facts** sheet with **66** questions intimidating. Students should be allowed no more than 10 minutes to complete the sheet. They should be asked to leave out any questions they do not know without counting or drawing.

The 45 facts on the 'Multiplication Pattern Facts' sheet are all learned as patterns – they do not require any memorization. The teacher should organize instruction so that students discover the following patterns (the order is not important, and the video starts with the 'twos' – it depends on the class). The patterns should not be taught but should be described by students (see video part 3 on the website). The students then become the teachers and the facts seem easier to learn. On the website there are six videos on teaching the multiplication facts. To watch the first four parts as one whole, go to <https://vimeo.com/10968680>

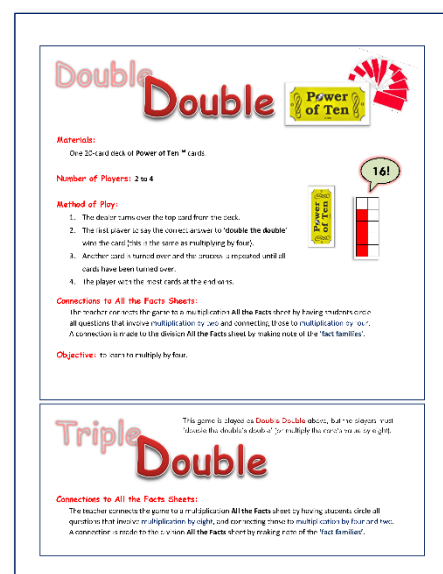
The order of the patterns is presented as follows but, in the videos, the first pattern a student identified as easy was the 'two times table' so that is where the day started.

- Zero
- One
- Two – which is the doubles pattern learned earlier in adding (may have been memorized)
- Ten
- Five – which is connected to ten

When a student knows these patterns, the teacher can encourage the student to connect the facts of four to the twos and then connect the facts of four to the eights by playing **Double-Double** and **Triple Double** games.



Click on 'page graphic' to access file. →



At this point the teacher moves to the **All the Facts** sheets and investigates the patterns in the facts of 9. Do not teach the finger rule for 9 because it is a trick that has no meaning for most teachers and students. Also, if you don't want to see adults using their fingers, why teach it?

# Multiplication Patterns – GETTING STARTED

Pre-All the Facts Sheet – **FORM A** (45)

|                 |                 |                 |                  |
|-----------------|-----------------|-----------------|------------------|
| $0 \times 1 =$  | $4 \times 5 =$  | $10 \times 1 =$ | $2 \times 6 =$   |
| $2 \times 3 =$  | $2 \times 10 =$ | $1 \times 4 =$  | $6 \times 0 =$   |
| $10 \times 9 =$ | $7 \times 2 =$  | $8 \times 5 =$  | $0 \times 10 =$  |
| $0 \times 2 =$  | $3 \times 5 =$  | $4 \times 0 =$  | $10 \times 6 =$  |
| $7 \times 5 =$  | $1 \times 5 =$  | $5 \times 0 =$  | $5 \times 6 =$   |
| $1 \times 7 =$  | $9 \times 2 =$  | $1 \times 8 =$  | $10 \times 10 =$ |
| $5 \times 9 =$  | $2 \times 4 =$  | $5 \times 2 =$  | $8 \times 2 =$   |
| $6 \times 1 =$  | $3 \times 10 =$ | $1 \times 3 =$  | $10 \times 7 =$  |
| $4 \times 10 =$ | $10 \times 8 =$ | $5 \times 5 =$  | $2 \times 1 =$   |
| $9 \times 0 =$  | $3 \times 0 =$  | $0 \times 8 =$  | $9 \times 1 =$   |
| $2 \times 2 =$  | $0 \times 7 =$  | $1 \times 1 =$  | $5 \times 10 =$  |
| $0 \times 0 =$  |                 |                 |                  |

## Analysis – FORM A

# Correct

# Left Out

# of Errors

Name \_\_\_\_\_

Date \_\_\_\_\_

Once the sheet has been marked and all errors circled, the student should:  
 [step 1] – **correct all errors** – these should have been circled by the teacher  
 [step 2] – do any questions that have been **left out**

QG : Multiplication Patterns Eng.

# Connecting the Patterns to the Remaining Facts

Pre-All the Facts Sheet – **FORM A** (21)

|                |                |                |                |
|----------------|----------------|----------------|----------------|
| $7 \times 8 =$ | $9 \times 6 =$ | $4 \times 4 =$ | $3 \times 4 =$ |
| $8 \times 9 =$ | $4 \times 8 =$ | $3 \times 7 =$ | $6 \times 8 =$ |
| $3 \times 3 =$ | $7 \times 4 =$ | $4 \times 6 =$ | $7 \times 7 =$ |
| $9 \times 4 =$ | $6 \times 7 =$ | $3 \times 9 =$ | $6 \times 6 =$ |
| $8 \times 3 =$ | $9 \times 9 =$ | $8 \times 8 =$ | $6 \times 3 =$ |
| $7 \times 9 =$ |                |                |                |

## Useful CONNECTORS – FORM A (8)

|                |                |                |                |
|----------------|----------------|----------------|----------------|
| $2 \times 8 =$ | $2 \times 2 =$ | $7 \times 2 =$ | $9 \times 2 =$ |
| $4 \times 2 =$ | $6 \times 2 =$ | $2 \times 5 =$ | $2 \times 3 =$ |

### Analyze Your Work – FORM A – Connecting the Patterns

# Correct

# Left Out

# of Errors

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

Name \_\_\_\_\_

Date \_\_\_\_\_

Once the sheet has been marked and all errors circled, the student should:  
*[step 1]* – **correct all errors** – these should have been circled by the teacher  
*[step 2]* – do any questions that have been **left out**

# Multiplication Patterns – GETTING STARTED

Pre-All the Facts Sheet – **FORM B** (45)

|                 |                   |                 |                  |
|-----------------|-------------------|-----------------|------------------|
| $1 \times 0 =$  | $5 \times 4 =$    | $1 \times 10 =$ | $6 \times 2 =$   |
| $3 \times 2 =$  | $10 \times 2 =$   | $4 \times 1 =$  | $0 \times 6 =$   |
| $9 \times 10 =$ | $2 \times 7 =$    | $5 \times 8 =$  | $10 \times 0 =$  |
| $2 \times 0 =$  | $5 \times 3 =$    | $0 \times 4 =$  | $6 \times 10 =$  |
| $5 \times 7 =$  | $5 \times 1 =$    | $0 \times 5 =$  | $6 \times 5 =$   |
| $7 \times 1 =$  | $2 \times 9 =$    | $8 \times 1 =$  | $10 \times 10 =$ |
| $9 \times 5 =$  | $4 \times 2 =$    | $2 \times 5 =$  | $2 \times 8 =$   |
| $1 \times 6 =$  | $10 \times 3 =$   | $3 \times 1 =$  | $7 \times 10 =$  |
| $10 \times 4 =$ | $8 \times 10 =$   | $5 \times 5 =$  | $1 \times 2 =$   |
| $0 \times 9 =$  | $0 \times 3 =$    | $8 \times 0 =$  | $1 \times 9 =$   |
| $2 \times 2 =$  | $7 \times 0 =$    | $1 \times 1 =$  | $10 \times 5 =$  |
| $0 \times 0 =$  | Analysis – FORM B |                 |                  |

# Correct

# Left Out

# of Errors

Name \_\_\_\_\_

Date \_\_\_\_\_

Once the sheet has been marked and all errors circled, the student should:  
 [step 1] – **correct all errors** – these should have been circled by the teacher  
 [step 2] – do any questions that have been **left out**

QG : Multiplication Patterns Eng.

# Connecting the Patterns to the Remaining Facts

Pre-All the Facts Sheet – **FORM B** (21)

|                |                |                |                |
|----------------|----------------|----------------|----------------|
| $8 \times 7 =$ | $6 \times 9 =$ | $4 \times 4 =$ | $4 \times 3 =$ |
| $9 \times 8 =$ | $6 \times 4 =$ | $7 \times 3 =$ | $8 \times 6 =$ |
| $3 \times 3 =$ | $4 \times 7 =$ | $6 \times 4 =$ | $7 \times 7 =$ |
| $4 \times 9 =$ | $7 \times 6 =$ | $9 \times 3 =$ | $6 \times 6 =$ |
| $3 \times 8 =$ | $9 \times 9 =$ | $8 \times 8 =$ | $3 \times 6 =$ |
| $9 \times 7 =$ |                |                |                |

## Useful CONNECTORS – FORM B (8)

|                |                |                |                |
|----------------|----------------|----------------|----------------|
| $8 \times 2 =$ | $2 \times 2 =$ | $2 \times 7 =$ | $2 \times 9 =$ |
| $2 \times 4 =$ | $2 \times 6 =$ | $5 \times 2 =$ | $3 \times 2 =$ |

### Analyze Your Work – FORM B – Connecting the Patterns

# Correct

# Left Out

# of Errors

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

Name \_\_\_\_\_

Date \_\_\_\_\_

Once the sheet has been marked and all errors circled, the student should:  
*[step 1]* – **correct all errors** – these should have been circled by the teacher  
*[step 2]* – do any questions that have been **left out**

# Double Double



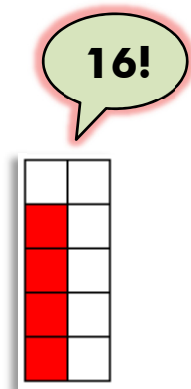
## Materials:

One 20-card deck of **Power of Ten™** cards.

## Number of Players: 2 to 4

## Method of Play:

1. The dealer turns over the top card from the deck.
2. The first player to say the correct answer to '**double the double**' wins the card (this is the same as multiplying by four).
3. Another card is turned over and the process is repeated until all cards have been turned over.
4. The player with the most cards at the end wins.



## Connections to All the Facts Sheets:

The teacher connects the game to a multiplication **All the Facts** sheet by having students circle all questions that involve **multiplication by two** and connecting those to **multiplication by four**. A connection is made to the division **All the Facts** sheet by making note of the '**fact families**'.

**Objective:** to learn to multiply by four.

# Triple Double

This game is played as **Double Double** above, but the players must 'double the double's double' (or multiply the card's value by eight).

## Connections to All the Facts Sheets:

The teacher connects the game to a multiplication **All the Facts** sheet by having students circle all questions that involve **multiplication by eight**, and connecting those to **multiplication by four and two**. A connection is made to the division **All the Facts** sheet by making note of the '**fact families**'.